Metamorphic Runtime Checking of Applications without Test Oracles

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ABSTRACT
Challenges arise in testing applications that do not have test oracles, i.e., for which it is impossible or impractical to know what the correct output should be for general input. Metamorphic testing, introduced by Chen et al., has been shown to be a simple yet effective technique in testing these types of applications: test inputs are transformed in such a way that it is possible to predict the expected change to the output, and if the output resulting from this transformation is not as expected, then a fault must exist.

Here, we improve upon previous work by presenting a new technique called Metamorphic Runtime Checking, which automatically conducts metamorphic testing of both the entire application and individual functions during a program’s execution. This new approach improves the scope, scale, and sensitivity of metamorphic testing by allowing for the identification of more properties and execution of more tests, and increasing the likelihood of detecting faults not found by application-level properties. We also present the results of new mutation analysis studies that demonstrate that Metamorphic Runtime Checking can kill an average of 170% more mutants than traditional, application-level metamorphic testing alone, and advances the state of the art in testing applications without oracles.

Categories and Subject Descriptors
D.2.4 [Software Engineering]: Software/Program Verification; D.2.5 [Software Engineering]: Testing and Debugging

General Terms
Reliability

Keywords
Software Testing, Test Oracle, Metamorphic Testing

1. INTRODUCTION
In the testing of software, a “test oracle” [41] is required to indicate whether the output is correct for the given input. Despite a recent interest in the testing community in creating and evaluating test oracles [49], still there are a variety of problem domains for which a practical test oracle does not exist in the general case. Applications in the fields of scientific computing, simulation, machine learning, etc. fall into a category of software that Weyuker describes as “Programs which were written in order to determine the answer in the first place. There would be no need to write such programs, if the correct answer were known” [54]. Thus, in the general case, it is not possible to know the correct output in advance for arbitrary input. In other domains, such as optimization, determining whether the output is correct is just as difficult as it is to derive the output in the first place, and creating an efficient, practical oracle may not be feasible.

Although some faults in such programs - such as those that cause the program to crash or produce results that are obviously wrong to someone who knows the domain - are easily found, and partial oracles may exist for a subset of the input domain, subtle errors in performing calculations or in adhering to specifications can be much more difficult to identify without a practical, general oracle.

Much of the recent research into addressing the so-called “oracle problem” has focused on the use of a technique called metamorphic testing [10] in domains such as bioinformatics [11], machine learning [32, 56], scientific computing [24], and simulation [12, 44]. As the name implies, in metamorphic testing changes are made to existing test inputs in such a way (based on the program’s “metamorphic properties”) that it is possible to predict what the change to the output should be. That is, if program input $I$ produces output $O$, additional test inputs based on transformations of $I$ are generated in such a manner that the change to $O$ (if any) can be predicted. In cases where the correctness of the original output $O$ cannot be determined, i.e., if there is no test oracle, program failure can still be detected if the change to $O$ is not as expected when using the new input.

Through our own past investigations into metamorphic testing [32, 33, 34], we have garnered three key insights. First, the metamorphic properties of individual functions are often different than those of the application as a whole. Thus, by checking for additional and different relationships, we can reveal defects that would not be detected using only the metamorphic properties of the full application. Second,
the metamorphic properties of individual functions can be checked in the course of executing metamorphic tests on the full application. This addresses the problem of generating test cases from which to derive new inputs, since we can simply use those inputs with which the functions happened to be invoked within the full application. Third, when conducting tests of individual functions within the full running application in this manner, checking the metamorphic properties of one function can sometimes detect defects in other functions, which may not have any known metamorphic properties, because the functions share internal application state.

In order to advance the state of the art in testing applications that do not have practical, general test oracles, this paper seeks to make metamorphic testing more effective by improving: the number and types of metamorphic properties that can be checked (scope); the number and types of metamorphic tests that are run for a single program input (scale); and the likelihood of revealing subtle faults that would not cause a violation of an application-level metamorphic property (sensitivity).

In order to realize these improvements, we present a solution based on checking the metamorphic properties of the entire application and those of individual functions (or methods, procedures, subroutines, etc.) as the full application runs. That is, the program under test is not treated only as a black box, but rather metamorphic testing also occurs within the application, at the function level, in the context of the running program. This will allow for the execution of more tests and also makes it possible to check for subtle faults inside the code that may not cause violations of the application's metamorphic properties.

In presenting this new solution, this paper makes three contributions:

1. A new type of testing called Metamorphic Runtime Checking (Section 4). This is a new approach that improves metamorphic testing in that metamorphic properties of individual functions, not only the entire application, are also specified and then checked as the program is running.

2. An architecture of a Metamorphic Runtime Checking framework called Columbus (Section 5). This architecture allows for checking both application-level and function-level metamorphic properties as the program runs.

3. The results of new studies that show that Metamorphic Runtime Checking is more effective than other techniques in detecting faults in programs without test oracles (by up to 123%) and more effective than traditional, application-level metamorphic testing (by up to 1,350%) (Section 6).

Although Metamorphic Runtime Checking does not preclude other testing approaches, and could presumably be applied to applications that do have oracles, the focus of this work is on those that do not.

2. BACKGROUND

Metamorphic testing [10] was introduced as a general technique for creating follow-up test cases based on existing ones, particularly those that have not revealed any faults, by reusing test cases to create additional test inputs whose expected outputs can be predicted. In metamorphic testing, if input x produces an output f(x), the function’s (or application’s) metamorphic properties can be used to guide the creation of a transformation function t, which can be applied to the input to produce t(x); this transformation then allows us to predict the output f(t(x)), based on the (already known) value of f(x). In the case where f has an oracle, then if we know that f(x) is correct, we could also know whether f(t(x)) is correct. Studies have shown that these additional test cases have fault-finding capabilities beyond that of the original test set [58].

For a simple example of metamorphic testing, consider a function that calculates the standard deviation of a set of numbers. Certain transformations of the set would be expected to produce the same result: for instance, permuting the order of the elements should not affect the calculation, nor should multiplying each value by -1. Furthermore, other transformations should alter the output, but in a predictable way: if each value in the set were multiplied by 2, then the standard deviation should be twice that of the original set.

Clearly metamorphic testing can be very useful in the absence of an oracle: even if it were not possible to know whether the initial output is correct, if the new output that results from transforming the input does not have the expected relationship with the original output, then a fault must exist in the implementation [13, 58]. Although satisfying these metamorphic properties does not indicate correctness, a violation of a property would indicate that one (or both) of the outputs is incorrect.

As an example from the domain of machine learning, anomaly-based network intrusion detection systems build a model of “normal” traffic based on previous observations, and then later look for outliers that may be indicative of an attack. The model may be created according to the byte distribution of incoming network payloads, since the distribution in worms, viruses, etc. may deviate from that of normal network traffic [53]. When a new payload arrives, its byte distribution is then compared to the model, and anything deemed anomalous causes an alert. When testing such a program, it may not be possible to know a priori whether a particular input should raise an alert, since it depends on the model. However, if while the program is running we take the new payload and randomly permute the order of its bytes, the result (anomalous or not) should be the same, since the model only concerns the distribution, not the order. If the result is not the same, and this property is violated, then a fault must exist in the implementation.

Despite recent successes in demonstrating that metamorphic testing can be effectively applied to real-world programs in domains for which there is no practical, general test oracle (e.g., [11], [12], [44], [56], etc.), there is still room for improvement when it comes to its ability to detect faults. By identifying more metamorphic properties (i.e., increasing the scope), deriving more test cases for each program input (increasing the scale), and checking for subtle faults that may not cause a violation of application-level metamorphic properties (increasing the sensitivity), we can make metamorphic testing even more effective.

Our solution is a new technique called Metamorphic Runtime Checking, further discussed in Section 4. In this approach, we check the metamorphic properties at the function level while conducting metamorphic testing at the system level. By running more tests with more inputs in more
Metamorphic Runtime Checking combines program-level metamorphic testing with function-level metamorphic checking, by performing such checking at runtime.

3. RELATED WORK

Metamorphic Runtime Checking can be considered a cross between metamorphic testing and runtime assertion checking [14], in that the metamorphic properties that are checked are analogous to program invariants: at the point in the program execution in which the function is called, its metamorphic properties are expected to hold, given the current function inputs and application state. Although we cannot know for certain just from observation that a given property will always hold, and satisfying the property does not indicate correctness, if the metamorphic property is ever violated then a fault has been revealed.

Although these approaches are similar, there are some key differences between metamorphic properties and program invariants. First, invariants and assertions address how variables relate to each other, or variable’s expected values, but do not describe the expected relations between outputs that result from multiple executions with transformed inputs. Additionally, in practice assertions typically are read-only and do not have side effects; in our approach, though, the properties rely on additional invocations of the functions, which are allowed to have side effects, but these side effects are contained so as not to affect the running program.

Metamorphic properties are similar in some ways to algebraic specifications [15], though algebraic specifications often declare legal sequences of function calls that should produce an expected result, but do not describe how a particular function should react when its input is changed. The runtime checking of algebraic specifications has been explored in [39] and [46], though neither work considered the particular issues that arise from testing without oracles. Other work in this area has focused on consistency checking of abstract data types [47], but has not sought to create oracles for applications that do not otherwise have them.

Recent work in metamorphic testing has focused on its applicability in different domains (e.g., [23, 44, 51]), but not on improving its general effectiveness in terms of scope, scale, and sensitivity. Beydeda [8] first brought up the notion of combining metamorphic testing and self-testing components, but did not investigate an implementation or consider the effectiveness on testing applications without oracles, as we do here.

Finally, the work presented here builds on our own preliminary research into function-level metamorphic testing [35] in two significant ways. First, in this paper we describe a new execution model (Section 4) and new framework architecture (Section 5) that allows for checking the function-level metamorphic properties in parallel with and in the same state as the original function execution, as opposed to running the test cases sequentially. Additionally, we present the results of new empirical studies (Section 6) comparing this new approach to other testing techniques, and investigate the particular benefits of using function-level metamorphic testing in addition to system-level testing.

4. APPROACH

Metamorphic Runtime Checking is an extension of our previous work in Automated Metamorphic System Testing [34], in which an application’s metamorphic properties are specified and then the program is executed multiple times: once with the original input, and then again for each of
the transformed inputs, according to the properties, after which the new outputs are compared to the original to determine whether any properties have been violated. Despite the demonstrated effectiveness of this approach, it does not utilize properties of individual functions, only those of the entire application.

In our new approach, additional metamorphic tests are logically attached to the functions for which metamorphic properties have been specified. Upon a function’s execution, the corresponding tests are executed as well: the arguments are modified according to the specification of the function’s metamorphic properties, the function is run again in the same application state as the original, and the output of the function with the original input is compared to that of the function with the modified input. If the result is not as expected according to the specified property, then a fault has been exposed.

As shown in Figure 1, the tester provides a program input to a Metamorphic Runtime Checking framework, which then transforms it according to the metamorphic property of the program P (for simplicity, this diagram only shows one metamorphic property, but a program may, of course, have multiple). The framework then invokes P with both the original input and the transformed input; as seen at the bottom of the diagram, when each program invocation is finished, the outputs can be checked according to the property.

While each invocation of P is running, though, metamorphic properties of individual functions can be checked as well. As shown on the left side of Figure 1, in the invocation of P with the original program input, before a function f is called, its input x can be transformed according to the function’s property to give t(x). The function is called with each input, and then f(t(x)) is evaluated according to the original value of f(x) to see if the property is violated.

Meanwhile, in the additional invocation of P (right side of the diagram), function-level metamorphic testing still occurs for function f, this time using input x’, which results from the transformed program input to P. In this case, f(t(x’)) and f(x’) are compared.

By incorporating function-level metamorphic properties into the testing, we can improve the scope and scale of metamorphic testing by running more tests using more properties and more inputs. In this example, if we used only the application-level property of P, we would run just one test. However, by also considering P’s functions, we can now check two properties and run a total of three tests. Additionally, this also allows us to improve the sensitivity of metamorphic testing by revealing subtle faults at the function level that may not violate application-level properties. Our study (described in-depth in Section 6.3) shows that this sensitivity gain can increase the effectiveness of metamorphic testing by up to 1,350% (on average, 170%).

In order to conduct Metamorphic Runtime Checking, the tester must first identify the metamorphic properties of the application to be tested and its constituent functions. This can be done manually, using domain knowledge or guidelines as presented in [32], or can be done automatically, as in [25].

Once the metamorphic properties have been determined, they must be expressed in such a way that the properties can be checked at runtime. In previous work, we discussed the use of configuration files for specifying application-level properties [34], and we have also explored using code annotations based on the Java Modeling Language [26] for function-level properties [35]. Any of these approaches can be used in Metamorphic Runtime Checking.

Last, testing can commence. Unlike in conventional unit testing, in Metamorphic Runtime Checking the tester need not construct any specific test harness; rather, metamorphic testing is conducted by simply executing the program with selected test inputs. The testing framework would allow for the checking of both application-level and function-level properties, and report any violations.

5. ARCHITECTURE

In this section we introduce the architecture of a testing framework for Metamorphic Runtime Checking, which we call Columbus.

5.1 Overview of Application-Level Testing

The Columbus framework is an extension of the Amsterdam framework for application-level metamorphic testing, which we introduced in our work on Automated Metamorphic System Testing [34] and is only summarized here.

In the Amsterdam framework, metamorphic properties of the entire application are specified using a configuration file. The framework executes the program with the original input, and then modifies the program inputs according to the properties. The program is then run again with the new inputs, but additional invocations are run in separate sandboxes so that they do not interfere with each other. Once all executions have finished, the outputs are checked according to the specified properties, and any violations are reported.

The Columbus framework builds upon Amsterdam by allowing testers to also specify function-level properties, and then by conducting additional metamorphic testing as the program invocations execute, as described below.

5.2 Function-Level Testing

In order to perform metamorphic testing of an individual function during the execution of the program, the Columbus framework needs to: execute the function with the original input and get the original output; transform the input according to the specified metamorphic property; call the function again, this time with the new input, but in the same application state as the original function call; and then get the new output and compare it to the original, again according to the specified property, to see whether the property was violated. All but the first of these steps would be repeated for each of the function’s specified properties.

One challenge is that the testing framework must ensure that the additional function invocations do not adversely affect the state of the running program: the goal is that the instrumented application should still produce the same output as an uninstrumented version, even though Metamorphic Runtime Checking is being conducted. For instance, assume that the program calls function f with input x, which is transformed according to the metamorphic property to t(x). In order for the program to continue to run as normal after the metamorphic tests have been run, the testing framework must ensure that the return value sent to the calling function is f(x), and not f(t(x)). Likewise, any side effect of calling f(x), such as modifying a global variable, must be permitted, but the framework must make sure that any side effect of calling f(t(x)) is hidden.

Since existing runtime assertion checking techniques (as
Figure 2: Model of Columbus framework for function-level metamorphic testing. Upon invocation of a function that Columbus will check, we fork execution to allow normal execution to continue while (in a sandbox) the input is transformed and the function is tested.

surveyed in [14]) and monitoring tools (such as Gamma [40]) do not support executing a function multiple times and do not safeguard against side effects, a new solution is required.

Figure 2 shows how the Columbus framework supports function-level metamorphic testing. First, the framework intercepts the call to function f, which can be accomplished through wrapping the function or by injecting code. Note that neither the signature of the function nor its return type is changed, and the calling function is never aware that metamorphic testing is being conducted.

Before the body of function f is invoked, the framework must create a “sandbox” so that the extra function calls do not affect the state of the running application. In native languages like C and C++, this can be accomplished by forking the process: the test inherits the state of the program at the time of the original function call, but does not affect it when the function is run a second time. In managed languages like Java and C#, for which forking the entire virtual machine is unwieldy, deep cloning (and using isolation techniques as described in [6]) can be used to make copies of all objects that may be affected. A new thread can then be spawned here, using references to the sandboxed/cloned objects, instead of the original.

Alternatively, a rollback mechanism could be used to execute the test case, record its results, restore the original state, and then execute the code with the original input.

In order to run the test, the input x to the function f is first modified according to the particular metamorphic property to give t(x). The transformation that should be applied to the input can be specified using code annotations [35], a configuration file, etc. Then the (instrumented) implementation of the function is invoked using this new input t(x).

In the original function call (right-hand side of Figure 2), the function f is invoked with the unmodified input x, and once it completes, the output f(x) can be logged or immediately shared with the test. If the tests run in a separate process from the original, then a mechanism like shared memory or message passing would need to be used here, otherwise this can be done with a global/static variable.

Once the test case has determined that the original function call has finished, e.g., using signals between processes or by using shared flags, the outputs f(x) and f(t(x)) are compared according to the metamorphic property. Just as the transformation required the specification of a function t, a function g must be specified for checking the outputs, and then the test can be indicated here by determining whether f(t(x)) = g(f(x)).

Finally, the test terminates, the output f(x) that results from the original input is returned to the calling function, and the rest of the program continues as normal.

5.3 Prototype Implementations

In order to conduct the experiments described in the following section, we created prototype implementations of the Columbus framework for both C and Java applications. For specifying the metamorphic properties and generating the test cases, we built upon our previous work [35] using code annotations based on the Java Modeling Language (JML) [26]. Listing 1 shows the specification of the properties for a standard deviation method in Java, using the examples described in Section 2. Keywords such as \permute and \multiply refer to built-in functions in the framework; other keywords for manipulating arrays or Collections include \reverse, \include, \exclude, \concatenate, \split, etc. Also, the \result keyword refers to the output of the original function call, as is standard in JML.

For creating the sandbox and sharing the function outputs, we modified the Invite framework used for “in vivo testing” [31], which allows for the execution of unit tests alongside a running program. We further reduced the performance overhead of sandboxing test executions using our tool for test case isolation, VmVm [6]. The overhead introduced by these tools is discussed in Section 6.4.

/*@
 @meta standardDev \permute (A) \result 
 @meta standardDev \multiply (A, -1) \result 
 @meta standardDev \multiply (A, 2) \result * 2 
*/
 double standardDev ( int A[] ) { . . . }

Listing 1: Specifying metamorphic properties of a standard deviation function in Java. Columbus uses a markup based on JML [26] to specify properties.

Although this prototype framework preserves the internal state of the application during function-level test execution, it does not currently prevent external side effects that may change the system, e.g., files, a database, the network, etc. A possible solution would be integration with a record/replay system such as Chronicler [7] to record execution of the program up to the point at which the metamorphic testing would be conducted, and then execute the tests later and/or in a different environment so that potential changes to the system do not affect the original program execution. This is left as future work.
6. EMPIRICAL STUDIES

To evaluate the effectiveness of Metamorphic Runtime Checking at detecting faults in applications without test oracles, we compare it to runtime assertion checking using program invariants. When used in applications without test oracles, assertions can ensure some degree of correctness by checking that function input and output values are within a specified range, the relationships between variables are maintained, and a function’s effects on the application state are as expected [38]. While satisfying the invariants does not ensure correctness, any violation of them at runtime indicates an error.

Although we are not aware of any other work that has specifically attempted to determine the “state of the art” for testing applications without oracles, runtime assertion checking is mentioned as a common and effective technique in the literature, e.g., Baresi and Young’s survey paper [4] on techniques for testing applications without test oracles, and Kanewala and Bieman’s paper [24] on testing programs used in computational science. Additionally, using invariant detection tools, this approach is easy to automate, and does not rely on a human tester, as do other approaches such as N-Version Programming or creating a formal specification.

6.1 Experimental Setup

The experiments described in this section seek to answer the following research questions:

1. Is Metamorphic Runtime Checking more effective than using runtime assertion checking for detecting faults in applications without test oracles?

2. What contribution do application-level and function-level metamorphic properties make to the effectiveness of Metamorphic Runtime Checking?

3. Is Metamorphic Runtime Checking suitable for practical use?

6.1.1 Target Applications

In these experiments, we applied both runtime assertion checking and Metamorphic Runtime Checking to nine real-world applications that are representative of different domains that have no practical general test oracles: supervised machine learning (classification, clustering, and ranking), data mining (information retrieval and topic modeling), discrete event simulation, and optimization. The applications include: C4.5 [43], a decision tree-based machine learning classification algorithm; GAFit [19], an optimization program that uses a genetic algorithm implemented to solve the bin-packing problem; JSim [45], a discrete event simulation engine developed at UMass Amherst; K-means [28], a clustering algorithm as implemented in the Mahout [5] framework; Latent Dirichlet Allocation (LDA) [9], a topic modeling algorithm, also as implemented in Mahout; Lucene [2], a text search engine library that is part of the Apache framework; MartiRank [20], a machine learning ranking algorithm, which was developed by researchers at Columbia University’s Center for Computational Learning Systems; PAYL [53], an anomaly-based intrusion detection system implemented by researchers in Columbia University’s Intrusion Detection System Lab; and Support Vector Machines (SVM) [52], a machine learning classification algorithm, as implemented in the Weka [55] open-source toolkit.

More detail about the applications is provided in Table 1. Note that for the Java applications, the information only includes the implementations of the specific algorithms, and not any underlying frameworks.

<table>
<thead>
<tr>
<th>Name</th>
<th>Domain</th>
<th>Language</th>
<th>LOC</th>
<th>Functions</th>
<th>Invariants</th>
<th># of Metamorphic Properties identified at the level of:</th>
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<td>C</td>
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<td>141</td>
<td>27,603</td>
<td>Application</td>
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<td>optimization</td>
<td>C++</td>
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<td>19</td>
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<td>Function</td>
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<td>Function</td>
</tr>
<tr>
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<td>clustering</td>
<td>Java</td>
<td>717</td>
<td>46</td>
<td>137</td>
<td>Function</td>
</tr>
<tr>
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<td>topic modeling</td>
<td>Java</td>
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<td>103</td>
<td>1,323</td>
<td>Function</td>
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<tr>
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<tr>
<td>MartiRank</td>
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<td>19</td>
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<tr>
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<td>anomaly detection</td>
<td>Java</td>
<td>4,199</td>
<td>164</td>
<td>19,730</td>
<td>Function</td>
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<td>Java</td>
<td>1,213</td>
<td>49</td>
<td>2,182</td>
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</tbody>
</table>

Table 1: Applications used in experiment. Applications were selected to be representative of different domains that have no practical test oracles. Invariants were identified using Daikon [18]; metamorphic properties were detected by hand.

6.1.2 Identifying Program Invariants

To create assertions, we used the Daikon invariant detection tool [18]. Daikon observes the execution of multiple program runs and creates a set of likely invariants, which can then be used as assertions for subsequent runs of the program. Although it is possible to customize the types of invariants that Daikon can detect, in our experiments we only use its out-of-the-box features. Note that the invariants created by Daikon only include function pre- and post-conditions, and do not incorporate any assertions that are within the function itself.

To create the set of invariants that we could use for runtime assertion checking, we applied Daikon to each application, using the following data sets as input: for SVM, C4.5, and K-means, 10 of the most popular data sets from the UC-Irvine repository of machine learning data sets [37]; for MartiRank, ten randomly generated data sets of various sizes; for PAYL, network traffic on our department’s LAN over a one-hour period; for Lucene and LDA, the corpus of Shakespeare’s comedies [30]; and for GAFit, a collection of 84 files ranging in size from 118 bytes to 14.9MB.
Figure 3: Results of mutation analysis, showing percentage of mutants killed by each approach. In several cases, Metamorphic Runtime Checking was far more effective than Runtime Assertion Checking, killing up to 123% more mutants.

6.1.3 Identifying Metamorphic Properties

To identify the application-level metamorphic properties for the experiment, we followed the guidelines set forth in [32], which categorizes the types of properties that applications in these domains tend to exhibit. Each property was verified with the data sets described above.

To identify function-level properties, we inspected the source code and hand-annotated the functions that we expected to exhibit the types of properties described in [32]. To ensure that the properties were not limited to only the ones that we could think of, some of the function-level metamorphic properties used in this experiment are based on those used in other, similar studies. In particular, the metamorphic properties of many machine learning and optimization applications have been documented elsewhere [5, 24, 57, 56], and some of the properties used for Lucene are based on those presented by Zhou et al. [59], in which the authors applied metamorphic testing to Internet search engines such as Yahoo!, Google, and Microsoft Live Search.

Although these properties were identified by hand, which introduces some threat to the validity of the experiment, we are not aware of any publicly available tool for automatically detecting properties (we currently are developing such a tool[50], however it is not yet sufficiently stable to use for such an experiment). However, numerous studies [22, 27, 29] have independently confirmed that these are the types of properties that tend to be identified by humans anyway, as do those involving machine learning-based approaches to property detection [25].

The total numbers of application-level and function-level metamorphic properties are listed in Table 1.

6.1.4 Methodology

To determine the effectiveness of the testing techniques, we used mutation analysis to systematically insert faults into the source code of the applications described above, and then determined whether the mutants could be killed (i.e., whether the faults could be detected) using each approach. Mutation analysis has been shown to be suitable for evaluation of effectiveness [1], and is generally accepted as the most objective mechanism for comparing the effectiveness of different testing techniques [17, 48].

Each mutated version of the program had exactly one mutation. Mutations that yielded a fatal runtime error (crash), an infinite loop, or an output that was clearly wrong (for instance, not conforming to the expected output syntax, or simply being blank) were discarded since any reasonable approach would detect such faults. We also did not consider “equivalent mutants” for which the inputs used in the experiment produced the same program output as the original, unmutated version, e.g., those mutants that were not on the execution path for any test case or that would not have been killed with a true oracle for these inputs.

For each mutated version, we conducted runtime assertion checking with the invariants detected by Daikon. If any invariant were violated, the mutant was considered killed. We then performed Metamorphic Runtime Checking on the same mutated versions to determine whether any of the specified metamorphic properties were violated. The inputs used for mutation analysis were the same as those used for detecting invariants and verifying metamorphic properties, so as to avoid any issues related to spuriousness (see Threats to Validity below).

6.2 Evaluation of Effectiveness

Here we answer the first research question: “Is Metamorphic Runtime Checking more effective than using runtime assertion checking for detecting faults in applications without test oracles?”

Table 2 and Figure 3 summarize the results of the first experiment. The variation in the number of mutants for each application is due to the different sizes of the source
Further analysis could more specifically characterize the types of faults each approach is most suitable for detecting, but it follows, then, that runtime assertion checking and Metamorphic Runtime Checking should be used together in the testing of applications without test oracles. When used in combination in our experiments, they were able to kill 95% of the mutants (totaling across all applications): only 88 of the 1,772 survived.

6.3 Contributions to Effectiveness

We now address the second research question: “What contribution do application-level and function-level metamorphic properties make to the effectiveness of Metamorphic Runtime Checking?”

Table 3 shows the results with the mutants grouped by (a) those that were killed only by application-level metamorphic properties, (b) those that were killed only by function-level properties, (c) those that were killed by both types of properties, and (d) those that were not killed by either one. We also show the relative improvement in number of mutants killed by combining both sorts of properties with Metamorphic Runtime Checking compared to using only application-level properties.

On average, we saw a 170% improvement in the total number of mutants killed when combining application-level properties with function-level properties. The variance in improvement was high, however, showing a strikingly high improvement of 1,350% in PAYL, while showing smaller improvement in C4.5 and MartiRank. Note that there was no improvement at all in the JSim and LDA applications, because application-level properties had already been able to kill all mutants. We believe that this improvement is attributed primarily to our increase in: the number of properties identified (scope); the number of tests run (scale); and the likelihood that a fault would be detected (sensitivity).

The improvement in the scope of metamorphic testing was particularly clear in the anomaly-based intrusion detection system PAYL. We were only able to identify two application-level metamorphic properties because it was not possible to create new program inputs based on modifying the values of the bytes inside the payloads (say, increasing them), since the application itself only allowed for particular syntactically and semantically valid inputs that reflected what it considered to be “real” network traffic. These two properties were only able to kill two of the 40 mutants. However, once we could use Metamorphic Runtime Checking to run metamorphic tests at the function level, we were able to identify many more properties that involved changing the byte arrays that were passed as function arguments, thus revealing 27 additional faults.

Likewise, we were able to increase the scale of metamorphic testing by running many more test cases. For instance, in MartiRank, even though we specified function-level properties for only a handful of functions, many of those are called numerous times per program execution, meaning that there are many opportunities for the property to be violated. A single execution of MartiRank consists of a number of “rounds” in which the set of input data is broken into sub-lists: there are N sub-lists in the Nth round, each containing 1/Nth of the total number of positive examples (i.e., examples with a label of 1). Each of the N sub-lists is sorted by each attribute, ascending and descending, and then MartiRank determines the attribute and sorting direc-
Table 3: Number of mutants killed by different types of metamorphic properties. For each application, we show the total number of mutants, then the number killed only by application-level metamorphic properties, those killed only by function-level properties, those that were killed by both sorts of properties, those killed by neither, and finally the percent improvement in performance of combining both techniques with Metamorphic Runtime Checking (MRC). No improvement was possible for JSim and LDA, as the application-level properties had already been able to kill all mutants.
RAM. On average, the performance overhead for the Java applications was around 3.5ms per test; for C, it was only 0.4ms per test. This cost is mostly attributed to the time it takes to create the sandbox and test process or thread. This impact can certainly be substantial from a percentage overhead point of view if many tests are run in a short-lived program. For instance, for C4.5, the overhead was on the order of 10x, even though in absolute terms it was well under a second. However, we point out that, for most the programs we investigated in our study, the overhead was typically less than a few minutes, which we consider a small price to pay for being able to detect faults in programs without a practical general test oracle.

Future work could investigate techniques for improving the performance of a Metamorphic Runtime Checking framework. Previously we considered an approach whereby tests were only executed in application states that had not previously been encountered, and showed that performance could be improved even when the functions are executed in distinct states up to 90% of the time [36]. It may be possible to reduce the overhead even more, for instance by reusing the results of previous tests, running tests probabilistically, etc.

6.5 Threats to Validity

In our study, we used Daikon to create the program invariants for runtime assertion checking. Although in practice invariants may typically be generated by hand, and some researchers have questioned the usefulness of Daikon-generated invariants compared to those generated by humans [42], we chose to use the tool so that we could eliminate any human bias or human error in creating the invariants. Additionally, others have independently shown that metamorphic properties are more effective at detecting defects than manually identified invariants [22], though for programs on a smaller scale than those in our experiment (a few hundred lines, as opposed to thousands as in many of the programs we used).

Daikon can generate spurious invariants if there are not enough program executions or if there are bugs in the code, but we mitigated this by using the same inputs for the mutation analysis experiment as for the generation of invariants and properties. Regardless of whether these “should” hold for the various functions, any violation of them would necessarily be coming from the inserted mutation, since they were never violated by those inputs in the unmutated version.

Last, the ability of metamorphic testing to reveal failures is clearly dependent on the selection of metamorphic properties, and the results may have varied had we used different ones instead. However, we have shown that a basic set of metamorphic properties can be used even without a particularly strong understanding of the implementation; the use of domain-specific properties may actually reveal even more failures [56]. We are actively developing a tool to dynamically detect likely metamorphic properties (using a mechanism comparable to Daikon [18]) which could mitigate this limitation, however, it is not yet sufficiently stable and validated to use for such a purpose [50].

7. FUTURE WORK

As mentioned above, the “sandbox” in our current implementation of the Columbus framework does not protect against modification of the external state, e.g., writing to a database or reading from the network. Although this was not an issue for the applications used in our experiments, future work could consider ways to make the sandbox more robust.

It may also be possible to apply Metamorphic Runtime Checking to non-functional aspects of the program by specifying properties related to the system state – such as heap memory usage, file descriptors, etc. – or “security invariants” [16] that, if violated upon subsequent function invocations, indicate a vulnerability. In our mutation analysis experiments, we noticed that some mutations affected whether or not memory was freed, caused buffer overflows, etc. but did not change the program output and thus were considered “equivalent mutants”. Metamorphic properties related to expected changes in system state may be able to detect such faults and vulnerabilities.

Finally, even though the applications studied in our experiment have no practical, general test oracle, some of their constituent functions certainly might, and conventional unit testing may be able to kill many of the mutations in the programs. Future research could investigate the effectiveness of combining traditional unit testing with Metamorphic Runtime Checking in such cases.

8. CONCLUSION

Metamorphic testing is an effective means of demonstrating faults in application domains without practical, general test oracles, such as machine learning, optimization, and scientific computing. In this paper, we have improved upon previous work in this area by introducing Metamorphic Runtime Checking, a new testing approach based on checking the metamorphic properties of both the entire application and its individual functions as the program runs. This paper has also described the architecture of a testing framework called Columbus.

As shown in our empirical studies, Metamorphic Runtime Checking is more effective than using runtime assertion checking, and has three distinct advantages over metamorphic testing using application-level properties alone. First, we are able to increase the scope of metamorphic testing, by identifying properties for individual functions in addition to those of the entire application. Second, we increase the scale of metamorphic testing by running more tests for a given input to the program. And third, we can increase the sensitivity of metamorphic testing by checking the properties of individual functions, making it possible to reveal subtle faults that may otherwise go unnoticed.

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10. REFERENCES

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